

The Attralucian Essays:
Exploring the Finite



First Edition

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The Attralucian Essays



Introducing the Functional Symbolic
Trajectory

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The Functional Symbolic Trajectory

Introducing the Functional Symbolic Trajectory

Words, Compression, and the Flow of Meaning in Finite Language

A word appears simple. We write *tree*, *number*, *force*, *attention*, *compression*, or *truth*, and the word seems to stand still. It appears to name something. It appears to hold a meaning. It appears to be a small symbolic object that can be placed into a sentence, moved around, defined, translated, indexed, or stored.

Yet this apparent stillness disappears as soon as we ask what the word is doing. A word opens into other words. Those words open into examples, memories, arguments, measurements, habits, drawings, equations, histories, conventions, disagreements, and repairs. The word does not remain a point. It begins to move.

This movement is not random. A word does not mean anything whatsoever. It is constrained by use, by mem-

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ory, by shared practice, by measurement, by the surrounding sentence, by the reader's prior experience, by the writer's intention, and by the wider body of language in which it appears. A word moves, but it moves within constraints.

This essay introduces the phrase *functional symbolic trajectory* as a way to describe that movement.

A functional symbolic trajectory is a finite symbolic path that performs usable work as it moves through context. A word is not treated as a fixed container of perfect meaning. It is treated as a symbolic compression whose meaning unfolds through use. The word is functional because it does something. It helps us point, count, measure, build, compare, remember, predict, persuade, calculate, coordinate, or question. It is symbolic because it exists as a finite mark, sound, gesture, token, sign, number, or other distinguishable form. It is a trajectory because it unfolds through time, use, context, and memory.

The phrase is intentionally plain. It does not require the reader to enter a specialised inherited vocabulary before the work can begin. It starts from a simple observation: words, signs, and symbols are not static objects. They are working paths.

This may sound obvious once stated. That is often the mark of a useful compression. The phrase makes visible something already present but not yet held with suffi-

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cient clarity. Many of the most important symbolic tools work in this way. They do not create the whole path by themselves. They compress a path that can later be unfolded.

The phrase “useful fiction,” associated with Bertrand Russell and related early twentieth-century work in logic and mathematics, performed this kind of compression. It allowed difficult abstractions to be handled as useful symbolic constructions without requiring them to be treated as ordinary physical things. The phrase helped loosen the grip of overly solid nouns. Yet from the present direction, the word *fiction* can also mislead. It may suggest that the symbol is merely invented, unreal, or dispensable. The issue being examined here is different. A symbol is not being dismissed as fiction. A symbol is being examined as a finite working trajectory.

This difference matters. A mathematical symbol, a scientific term, a technical word, or an everyday phrase may be constructed, compressed, unstable, incomplete, and uncertain while still being profoundly useful. Its value lies not in being a perfect object, but in carrying a usable path through a symbolic space.

The aim of this essay is to present the functional symbolic trajectory as a practical working idea. It will be placed in a historical path beginning with marks, counting, geometry, and mathematical notation; then positioned beside Russell’s useful or logical fictions; then connected

to Shannon's information theory and the modern engineering word *compression*; then developed into a formal sketch; and finally linked to nonlinear dynamics, artificial intelligence, language models, and the five pillars method used in Geofinitism/FSM.

The essay itself should be read as a trajectory. It begins with ordinary words, moves through historical compression, enters a formal symbolic frame, and returns to practical reading, writing, science, mathematics, and artificial intelligence.

Words do not stand still

The easiest way to enter the idea is to choose a familiar word and watch what happens.

Take the word *force*. In ordinary speech, *force* may mean strength, pressure, coercion, violence, intensity, or necessity. In Newtonian mechanics, force is commonly written as $F = ma$, where F is force, m is mass, and a is acceleration. In engineering, force may be associated with loads, stresses, mechanisms, instruments, and safety margins. In law or politics, force may refer to compulsion. In Finite Mechanics, force may be treated not as an isolated entity but as part of a finite identity involving mass, acceleration, and interaction.

The word has not become meaningless because it moves. It remains usable because each setting constrains the

path. The word *force* does not carry one perfect meaning that is simply unpacked in every situation. Instead, it begins a constrained movement through the symbolic space in which it is being used.

The same is true of *attention*. In everyday language, *attention* suggests focus, care, awareness, or conscious selection. In Transformer architectures, however, “attention” refers to a computational process involving projections of token embeddings into query, key, and value vectors, followed by pairwise similarity operations and recombination. The ordinary word pulls the reader toward human focus, but the mechanism is geometric and computational. This mismatch was central to the earlier work on pairwise phase-space embedding, where the so-called attention mechanism was reframed as a form of relational reconstruction over token sequences rather than human-like focus. The uploaded paper explicitly presents token sequences as ordered symbolic data and compares attention-like pairwise operations with phase-space reconstruction methods from nonlinear dynamics.

The word *attention* therefore becomes an example of the problem. It is functional, but it carries inherited motion. It can help a field develop quickly because it provides an intuitive phrase. It can also misdirect thought because the ordinary path of the word does not match the mechanism being described.

This is not unusual. It is how words work. Every useful

word has a history. Every technical word carries residues of older use. Every definition is an attempt to stabilise a movement that cannot be made perfectly still.

A word, then, is not best understood as a symbolic stone. It is better understood as a symbolic path that can be followed, repaired, redirected, sharpened, or abandoned.

This is the first working statement of the essay:

A word is a finite symbolic compression that unfolds as a functional trajectory in context.

Why the phrase is needed

The phrase *functional symbolic trajectory* is introduced because many existing words already carry too much inherited motion. Words such as *meaning*, *reference*, *truth*, *representation*, *model*, *fiction*, and *information* are useful, but each pulls the reader into older patterns of thought. These older patterns are not wrong in any simple sense. The problem is that they may begin the journey from the wrong place.

The present work begins from finite symbols in use. A mark is made. A sound is heard. A token is distinguished. A measurement is recorded. A sentence is written. A reader follows. A model predicts. A calculation returns. A symbol either functions well enough, or it fails, slips, branches, or needs repair.

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The phrase has three parts.

The word *functional* says that the symbol performs work. It is not being treated as decoration. A word may coordinate action, support calculation, compress a memory, direct attention, preserve a measurement, label a category, or guide a model. Its use is judged by what it enables.

The word *symbolic* says that the work is carried by finite distinguishable forms. These may be marks, sounds, gestures, numbers, diagrams, equations, code, tokens, or other forms that can be used and repeated. The symbol is finite because it appears within a bounded act of distinction. It is not the whole world. It is a usable sign within a symbolic system.

The word *trajectory* says that the symbol unfolds. It has path, direction, memory, and context. It may remain narrow under strong constraints, as in a formal calculation. It may widen in everyday conversation. It may branch in literature. It may become unstable in political speech. It may be sharpened by measurement. It may be changed by new instruments.

Together, the phrase describes a symbol that does work by moving through a constrained symbolic space.

A short definition can therefore be given:

A functional symbolic trajectory is a finite symbolic path that carries usable structure through context, under con-

straint, with uncertainty.

This definition is not intended to be perfect. It is intended to be good enough to begin the work. It can be refined as the path develops.

Marks, counting, and early symbolic compression

Human symbolic life begins with marks, counts, gestures, and repeated signs. A tally mark is not the sheep, the debt, the day, or the exchange. It is a compression of a relation that matters. One mark may stand for one animal, one unit of grain, one completed action, or one owed quantity. The mark allows the event to be carried forward.

This is already a functional symbolic trajectory. The mark begins in an event, passes through a symbolic act, and later returns as memory, comparison, settlement, or calculation.

Early counting systems, clay tokens, abaci, written numerals, and bookkeeping practices show that symbols did not emerge as detached abstractions. They were working tools. They compressed repeated acts into forms that could travel across time and between people.

A numeral is especially important. The symbol “5” is small, but it carries a long trajectory. It can refer to five

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sheep, five coins, five metres, five volts, five iterations, five dimensions in a model, or the fifth item in a sequence. The symbol is stable enough to be widely useful, but it does not perform the same work in every setting. It moves according to the system in which it is placed.

The history of mathematical notation shows this repeatedly. Symbols become powerful when they compress work that was previously slow, verbal, or difficult to repeat. A compact symbol can stabilise a movement, allowing the movement to be taught, copied, extended, and combined with other symbolic movements.

Robert Recorde's equals sign is a striking example. Before a compact sign for equality became common, equality could be written in words or expressed by longer phrases. Recorde's "=" compressed a judgement of sameness, balance, comparison, and substitutability into a mark. The symbol did not merely save space. It changed the ease with which symbolic work could be carried out.

The equals sign is therefore not simply a mark. It is a highly stabilised functional symbolic trajectory. It directs the reader to perform a relation. It says that what appears on one side and what appears on the other side are to be treated as equivalent under the rules being used. It is small because its history has been compressed.

The same can be said of algebraic symbols. The letter x in an equation is not a hidden object sitting behind the

page. It is a movable placeholder inside a constrained symbolic process. Its function depends on the rules of the system, the equation in which it appears, the operations allowed, and the goal of the calculation.

A symbol becomes powerful when a large amount of work can be compressed into a small finite form without losing enough structure to make the symbol fail.

Geometry as constructed trajectory

Geometry provides another early example. A geometrical figure can be treated as a noun: triangle, square, circle, line. But in classical geometrical practice, the figure is not merely named. It is constructed.

A circle is drawn by a permitted action. A line is extended. A triangle is formed. A square is built from relations among equal sides and right angles. The meaning is carried not only by the final figure but by the construction path.

This matters because it shows that symbolic meaning was never only about naming. It was also about permitted movement. The geometer does not merely say “square.” The geometer gives or assumes a path by which the square can be constructed, recognised, compared, and used.

A square is therefore a compressed construction. The

word *square* hides a path of operations. The diagram hides rules of production. The figure appears static only because the construction has been stabilised and compressed.

This connects directly to the present phrase. A functional symbolic trajectory may end in an apparently stable symbol, but the symbol carries a hidden path. To understand the symbol, one must often recover enough of that path to use it correctly.

A proof works in the same way. A proof is not a pile of statements. It is a constrained symbolic path from assumptions to conclusion. Each step must be allowed. Each transformation must be recognised by the rule system. The conclusion is not merely the final line; it is the final point of a permitted trajectory.

Mathematics, in this framing, is not weakened. It is clarified. It becomes a highly constrained practice of symbolic trajectory construction.

Russell's useful fiction and the need for a different path

The phrase “useful fiction” is important because it recognises that some symbolic constructions may work without being treated as ordinary objects. Russell's work, and the wider early twentieth-century effort to clarify mathe-

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matics through logic and symbolic analysis, helped show that many expressions can be transformed, analysed, or treated as constructions rather than as simple names of things.

The present essay does not reject that movement. It learns from it. The useful fiction loosens the grip of the noun. It tells us that a symbol may function without needing to be treated as a simple object.

However, the word *fiction* can pull the reader in an unhelpful direction. It may suggest that the symbolic construction is merely made up, or that its usefulness is somehow secondary to its lack of ordinary objecthood. The present work turns the question. It does not ask whether the symbol is fictional. It asks how the symbol functions, how it was compressed, how it moves, what constrains it, what uncertainty it carries, and whether it can return to measurement, prediction, construction, or shared use.

This shift is important for Geofinitism/FSM. A symbol does not need to be judged by whether it is a perfect copy of something outside the symbolic system. It can be judged by whether it functions as a finite symbolic trajectory. Does it carry usable structure? Does it coordinate? Does it predict? Does it calculate? Does it return to measurement? Does it remain stable under repeated use? Does it expose its uncertainty? Does it permit repair?

The phrase *functional symbolic trajectory* therefore keeps the useful part of “useful fiction” while changing the emphasis. It does not centre fiction. It centres function, symbol, and movement.

Shannon, information, and the engineering of compression

The modern word *compression* gained much of its technical force through information theory and the engineering of communication. Claude Shannon’s 1948 paper, “A Mathematical Theory of Communication,” made it possible to analyse communication systems in terms of signals, channels, noise, coding, uncertainty, and transmission. Shannon’s framework was extremely powerful because it separated the engineering problem of communication from ordinary questions about human meaning.

This separation was a strength. Engineers could ask how many bits were needed to transmit a message, how much redundancy was present, how noise affected a channel, and how coding could improve transmission. The theory enabled practical work in telecommunication, storage, coding, error correction, and computation.

The word *information* then began to travel. It moved from engineering into biology, computing, linguistics, psychology, physics, and everyday speech. As it travelled,

it carried Shannon's compression with it. This created enormous practical success, but also some confusion. A measure designed for signal transmission could be mistaken for a complete theory of meaning. A powerful engineering compression could be carried into settings where human symbolic trajectories were much wider than the channel model alone.

Compression in modern computing became one of the central mechanisms of the digital world. Files are compressed for storage. Images are compressed for transmission. Sound is compressed for streaming. Video is compressed so that moving images can cross networks. Text is compressed in archives. Data packets are compressed in communication systems. Machine learning systems compress large histories into parameters, embeddings, weights, and latent structures.

There are two broad kinds of compression that matter here.

In lossless compression, the original symbolic sequence can be recovered exactly. A text file compressed into a ZIP archive can be decompressed back into the same text file, provided the process works correctly. Huffman coding, arithmetic coding, and Lempel-Ziv methods belong to this family of exact symbolic recovery.

In lossy compression, the original is not recovered exactly. Instead, selected structure is preserved while other detail

is discarded. JPEG image compression, MP3 sound compression, and many video codecs work in this way. The goal is not perfect recovery. The goal is useful reconstruction under constraint.

This distinction is essential for language.

A word is not lossless. When the word *tree* is spoken, the listener does not decompress the exact same inner image, history, smell, species, childhood memory, ecological relation, and botanical structure that the speaker had in mind. The listener reconstructs a usable trajectory from the symbol, context, and prior history.

Language is therefore closer to lossy symbolic compression, but even this comparison is incomplete. A JPEG image is usually intended to reconstruct something like a particular image. A word does not decompress into one original object. It unfolds into a context-dependent path.

The word *compression* itself has therefore changed. It began in ordinary usage as pressing together or making smaller. It became a precise engineering term in communication and computing. It now also provides a powerful way to understand symbols, language, theories, and models. A word compresses history. A name compresses a person. A theorem name compresses a proof. A scientific model compresses measurements and permitted operations. A book title compresses a whole work. A phrase such as “useful fiction” compresses a larger in-

tellectual path. The phrase “functional symbolic trajectory” compresses the present one.

JPEG, curvature, and compression across scale

JPEG is a useful bridge because it makes compression visible. In ordinary digital images, a large amount of pixel-level information is present. Baseline JPEG divides the image into blocks, transforms local image data into frequency-like components using the discrete cosine transform, quantises those components, and then encodes the result. The process keeps some structures more strongly than others. Broad visual patterns tend to survive better than fine detail when compression is increased.

This is not merely a way of making files smaller. It is a way of deciding what structure matters enough to preserve under constraint.

In practical terms, JPEG separates broad variation from rapid local variation. It preserves a reconstruction that remains useful to human vision even though some detail has been removed. JPEG2000 and other methods use different tools, including wavelet-based approaches, but the wider lesson is similar: compression works by measuring structure at some scale, preserving selected relations, and allowing other relations to weaken or vanish.

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This provides a bridge to language. A word does not preserve every detail of the history compressed into it. It preserves enough structure for use. A definition does not preserve every use of a word. It selects and stabilises a path. A theory does not preserve every measurement or possible description. It compresses a body of relations into a form that can be used.

This also connects to the earlier work on compressed embeddings. When an embedding is compressed, the available trajectory of a model may change. Compression is not merely storage reduction. It can alter the geometry through which later reconstruction occurs. If the compression changes local relations, the model may follow a different path.

This leads to an important working sentence:

Compression is not only a reduction of size. Compression is trajectory shaping.

Once this is seen, words, equations, models, images, and embeddings can be placed into a shared frame. Each is a finite symbolic or signal structure that preserves selected relations while discarding or weakening others. Each must later be reconstructed in use. Each reconstruction carries uncertainty. Each may function well enough, fail, or drift.

The central proposal

The central proposal can now be stated more fully.

A functional symbolic trajectory is a finite symbolic movement that carries usable structure through context, under constraint, with uncertainty.

This proposal has several parts.

First, the symbol is finite. It appears as a distinguishable mark, sound, gesture, token, number, diagram, or other usable form. It is not the whole of what it may later evoke.

Second, the symbol is compressed. It carries more than its immediate form. The word *electron* compresses experiments, equations, instruments, textbooks, images, debates, measurements, and practices. The word *democracy* compresses histories, institutions, ideals, conflicts, procedures, and emotional commitments. The word *compression* compresses physical pressing, engineering coding, file storage, signal reduction, and symbolic reconstruction.

Third, the symbol unfolds. It does not remain inert. It begins a movement in the reader, listener, machine, calculation, or social setting. That movement may be narrow and controlled, as in a formal equation. It may be broad and unstable, as in political language. It may be highly trained, as in technical practice. It may be

fragile, as in new theory.

Fourth, the symbol is constrained. It is held by grammar, notation, measurement, training, tools, examples, prior use, and shared correction. The trajectory may move, but it does not move without structure.

Fifth, the symbol carries uncertainty. No finite symbol can carry the whole of its use-history without loss. No reader reconstructs exactly the same path. No definition permanently fixes every future use. The question is not whether uncertainty exists. The question is whether it is small enough, visible enough, and constrained enough for the symbol to function.

The functional symbolic trajectory is therefore neither a free metaphor nor a rigid definition. It is a working model of symbolic use.

A formal sketch

A light formal sketch can help stabilise the idea. The formalism is not intended to replace the prose. It is intended to make the relations easier to inspect.

Let S_α denote a finite symbolic space available at a symbolic resolution α . Here, S_α is the set of distinguishable symbols, marks, tokens, or symbolic states available to a user or system at that resolution. The parameter α denotes the minimum effective distinction being used in

the symbolic system. In later Geofinite work, α may be linked to the Alphonic Limit, but here it simply marks finite symbolic resolution.

Let $w \in S_\alpha$ denote a word or symbol. Let C denote the current context in which the symbol appears. Let H_w denote the history of prior uses, examples, measurements, documents, and practices associated with w . Let R denote the rule constraints, including grammar, notation, mathematical rules, institutional conventions, or operational procedures. Let δ denote the uncertainty associated with reconstructing or using the symbol.

We may then write the functional symbolic trajectory of w as:

$$\gamma_w = T(w; C, H_w, R, \alpha, \delta)$$

In this expression, γ_w denotes the trajectory activated by the symbol w . The function T denotes the process by which the symbol becomes a working path under the given conditions. The semicolon separates the symbol w from the conditions under which it is being used. The variables C , H_w , R , α , and δ declare that the trajectory is not produced by the symbol alone.

For a sequence of words or symbols,

$$W = (w_1, w_2, \dots, w_n)$$

where W is a finite ordered sequence and w_i is the i -th symbol in the sequence, we may define a coupled symbolic

trajectory:

$$\Gamma(W) = (\gamma_{w_1}, \gamma_{w_2}, \dots, \gamma_{w_n})$$

Here, $\Gamma(W)$ denotes the trajectory of the whole sequence. It is not merely the sum of isolated word trajectories, because each word changes the path of nearby words.

To express this local coupling, let k denote the number of neighbouring symbols considered on either side of w_i . The local neighbourhood of w_i is then:

$$N_k(w_i) = (w_{i-k}, \dots, w_{i-1}, w_i, w_{i+1}, \dots, w_{i+k})$$

where $N_k(w_i)$ denotes the local symbolic neighbourhood around w_i . At the beginning or end of a sequence, the neighbourhood may be shortened or padded depending on the system being used.

The trajectory of w_i can then be written as:

$$\gamma_{w_i} = \Phi(w_i; N_k(w_i), C, H_{w_i}, R, \alpha, \delta)$$

Here, Φ denotes the local trajectory-forming process. This expression says that the trajectory of a word depends on the word itself, its neighbouring symbols, the current context, its history, the relevant rules, the symbolic resolution, and uncertainty.

This captures a key point: words bend one another.

A symbol may also be understood as a compression of a wider history. Let C_{sym} denote symbolic compression, and let H_w denote the wider use-history of w . We may write:

$$C_{\text{sym}}(H_w) \rightarrow w$$

This means that the finite symbol w compresses a wider history H_w . The arrow does not mean perfect reduction. It means that a larger history is being carried forward in a smaller symbolic form.

Reading, interpretation, calculation, or model continuation can then be described as reconstruction. Let D_{sym} denote symbolic reconstruction. Then:

$$D_{\text{sym}}(w; C, H_r, R, \alpha, \delta) \rightarrow \hat{\gamma}_w$$

Here, H_r denotes the reader's, listener's, or system's available history, and $\hat{\gamma}_w$ denotes the reconstructed trajectory. The hat symbol over γ indicates that this is a reconstruction, not a perfect recovery of some original path.

This is important. The writer's intended trajectory and the reader's reconstructed trajectory may differ:

$$\gamma_w \neq \hat{\gamma}_w$$

However, communication may still succeed if the difference is small enough for the task. Let E denote the divergence between the intended or source trajectory γ_w

and the reconstructed trajectory $\hat{\gamma}_w$. We may write:

$$E = d(\gamma_w, \hat{\gamma}_w)$$

where d is a distance or difference measure appropriate to the symbolic system. Communication or symbolic use succeeds when E remains within an acceptable tolerance ϵ :

$$E \leq \epsilon$$

Here, ϵ denotes the maximum tolerated divergence for the task. In casual conversation, ϵ may be large. In a mathematical proof, engineering drawing, medical instruction, or computer program, ϵ may be very small.

This gives a practical way to think about symbolic success. A word does not need to carry perfect meaning. It must carry a trajectory that can be reconstructed closely enough for the purpose at hand.

Trajectories and nonlinear dynamics

The word *trajectory* is not chosen accidentally. In nonlinear dynamics, a trajectory is a path through a state space. The system changes over time. Its future path may depend on its current state, its prior path, and the structure of the space through which it moves. Some regions may attract repeated behaviour. Some small

changes may lead to larger divergences. Some systems may be stable in one region and unstable in another.

Language shows many similar features.

A sentence is not a bag of words. It is an ordered movement. The effect of a word depends on what came before and what may come after. The phrase “once upon a time” pulls the reader toward a familiar kind of continuation. The phrase “in conclusion” prepares the reader for closure. The phrase “ladies and gentlemen” begins a public address. The phrase “useful fiction” carries a historical and technical path. The phrase “functional symbolic trajectory” is intended to begin a different path.

Some phrases act as attractors. They pull continuation in certain directions. Others act as hinges. They turn a path. A single word may redirect a conversation. A technical term may stabilise a whole field. A misleading name may keep a field inside a poor explanation for decades.

This is why the earlier phase-space work matters. In that work, language was treated as an ordered symbolic sequence capable of being unfolded geometrically through methods related to delay embedding and pairwise comparison. The paper used simple examples to show how a sentence could be treated as a time series and then embedded as a trajectory. It also argued that Transformer attention should be understood less as human-like focus

and more as a relational geometry constructed over token sequences.

The present essay generalises that direction. The claim is not only that a machine model can process token sequences geometrically. The broader claim is that language itself can be usefully described as symbolic movement under constraint.

A simple illustration can be made using Takens-style delay coordinates. Suppose a sentence is converted into a finite scalar sequence:

$$x = (x_1, x_2, \dots, x_n)$$

where x is the full sequence, n is the number of measured positions, and x_i is a scalar measurement associated with the i -th word. For example, x_i might be the word length, syllable count, frequency rank, or another finite measurable property.

A three-dimensional delay embedding can be formed by choosing a delay τ , where τ is a positive integer giving the step between delayed measurements. The delay vector at position i is:

$$X_i = (x_i, x_{i+\tau}, x_{i+2\tau})$$

where X_i is a point in three-dimensional space. As i increases, the points X_i form a trajectory.

This does not claim that word length contains the whole

meaning of a sentence. It does not. The point is simpler and more basic: even a crude finite measurement of an ordered symbolic sequence can be unfolded into a visible path. Order creates geometry. Change the order and the path changes.

This gives a direct visual demonstration of the functional symbolic trajectory. A sentence is not merely a row of tokens. It is a path through symbolic measurement space.

Compression, reconstruction, and modern artificial intelligence

Modern artificial intelligence makes the trajectory-like nature of language harder to ignore. Large language models process sequences of tokens, learn statistical and geometric relations among them, and generate continuations. Whatever one thinks such systems are doing internally, their behaviour shows that language has strong continuation structure. The next token is not arbitrary. The path constrains what can follow.

A language model is trained on large bodies of text. That training compresses patterns of use into parameters and internal representations. The model does not store language as a list of fixed meanings. It develops a structure that can generate symbolic continuations under context. The result is not a perfect recovery of truth or intention.

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It is trajectory continuation under learned constraint.

This does not make machine language identical to human language. Human symbolic trajectories include bodies, instruments, social life, memory, goals, fear, humour, fatigue, touch, history, and practical action in the world. A machine model has a different path and different constraints. But both reveal the same basic issue: language cannot be fully understood as static word objects.

This is where compression becomes central. Modern AI systems compress text histories into model weights, embeddings, activations, attention-like matrices, and latent structures. These compressions shape the possible continuations. Change the compression and the trajectory changes.

The same is true in data transfer. Compress an image too aggressively and edges blur, textures vanish, and artefacts appear. Compress sound too aggressively and timbre changes. Compress video too aggressively and motion becomes blocky or smeared. Compress language too aggressively and nuance collapses. Compress embeddings in the wrong way and model behaviour may shift.

Thus, compression is not neutral. Compression determines what relations survive.

In ordinary information engineering, this is well understood. Compression must preserve what matters for the intended reconstruction. In symbolic language, the same

lesson applies. A word, phrase, definition, or theory compresses a wider structure. It preserves some relations and discards or weakens others. The resulting trajectory may still work, but only if the preserved structure is sufficient for the task.

This gives a way to understand why new terms are needed. A new term is not introduced merely to sound novel. It is introduced when existing compressions preserve the wrong structure or pull the reader along the wrong path.

The phrase “attention” in machine learning is a good example. It worked as an intuitive engineering compression. It helped name a mechanism. But it preserved too much of the ordinary human sense of attention and too little of the underlying geometric operation. The phrase “pairwise phase-space embedding” was introduced in the earlier work to redirect the path toward nonlinear reconstruction and relational geometry.

Likewise, the phrase “functional symbolic trajectory” is introduced because words such as *meaning*, *concept*, *representation*, and *fiction* do not quite preserve the structure needed here. They pull the reader into older compressed paths. The new phrase attempts to preserve function, symbol, movement, constraint, and uncertainty in one compact form.

Rewriting the five pillars as trajectory tests

The five pillars can be rewritten in the language of functional symbolic trajectories. This turns them into practical tests for examining a word, phrase, model, equation, or theory.

The first pillar is to identify the symbolic trajectory. Instead of asking only “what does this word mean?” we ask: what path is this symbol asking the reader to follow? Is the trajectory mathematical, historical, practical, emotional, institutional, computational, or mixed? What direction does the symbol create?

The second pillar is to locate the compression. What has been compressed into the symbol? A word may compress measurements, metaphors, assumptions, prior theories, instruments, social agreements, hidden histories, or unresolved disputes. A mathematical symbol may compress a construction. A scientific constant may compress an experimental practice. A technical term may compress a whole field.

The third pillar is to examine the construction path. How was the symbol built? What operations, measurements, examples, definitions, or repeated uses stabilised it? Can the path be reconstructed? Does the symbol return to marks, measurements, instruments, calculations,

or shared practice? Or does it float free of its construction?

The fourth pillar is to find the uncertainty or slippage. Where does the trajectory widen? Where do readers begin to diverge? Where does a word carry incompatible histories? Where is a finite value being introduced through a symbol that appears more certain than it is? Where does an abstraction silently replace a measurement?

The fifth pillar is to test functional return. Does the trajectory return to usable work? Can it predict, coordinate, measure, calculate, build, repair, or clarify? If the trajectory cannot return to function, then its symbolic compression may be ornamental, unstable, or misleading.

These five tests do not demand perfection. They ask whether the trajectory works well enough and whether its limits can be seen.

This is especially important for inherited scientific and mathematical language. Many words are so familiar that they appear natural. But familiarity is often compressed history. A word may feel obvious because its path has been walked many times. That does not make it perfect. It makes it stabilised.

The five pillars help slow the reader down. They ask the reader to inspect the path rather than merely accept the

noun.

Mathematics as constrained symbolic trajectory

Mathematics can be understood as one of the most constrained forms of symbolic trajectory construction. Its strength lies in the restriction of permitted moves. A mathematical expression is not simply read in an ordinary way. It is transformed according to rules.

Consider the equation:

$$F = ma$$

Here, F denotes force, m denotes mass, and a denotes acceleration. The expression is compact, but it carries a large trajectory. It compresses measurement practices, units, idealisations, historical development, and permitted calculations. In a Newtonian setting, it functions extremely well. In other settings, it may need modification, reinterpretation, or replacement.

The equation is not weakened by recognising it as a functional symbolic trajectory. On the contrary, its power becomes clearer. It works because its symbols, units, and transformations are tightly constrained. The tolerance ϵ for divergence is small. The allowed operations are well trained. The return to measurement is strong.

A proof has the same character. It is a symbolic trajectory whose steps are constrained by accepted rules. A proof succeeds when the reader can reconstruct the path and agree that each step is allowed. If a step is unclear, the trajectory breaks. If a term changes meaning mid-proof, the trajectory slips. If an assumption is hidden, the compression may fail.

This framing also helps explain why mathematical symbols can travel across centuries. They survive because their trajectories can be reconstructed by trained readers. The marks remain small, but the path remains teachable.

Science as measurement-constrained symbolic trajectory

Scientific work can be described as symbolic trajectory construction constrained by measurement. A theory compresses measurements, instruments, models, equations, assumptions, and predictions into a usable symbolic path. It is not the measured world itself. It is a finite symbolic structure that must repeatedly return to measurement.

This return is essential. Without return, the symbolic trajectory may become internally elaborate but externally weak. With return, the trajectory can be corrected, sharpened, rejected, extended, or replaced.

A scientific term such as *electron*, *gene*, *temperature*, *mass*,

field, *energy*, or *black hole* carries both measurement and history. These words are not simple labels. They are dense compressed trajectories. Each one connects instruments, equations, experiments, diagrams, institutional training, and public imagination.

The more successful the word becomes, the more solid it may appear. Yet this solidity is an achievement of repeated stabilisation. It is not the absence of trajectory. It is a well-repeated trajectory.

This matters when a new framework is introduced. New work often fails not because it is necessarily wrong, but because its symbolic trajectories have not yet been walked enough times. The reader has no stable path. The words are heard as strange, excessive, or unnecessary. The task of exposition is therefore not merely to define terms. It is to build walkable trajectories.

This is one reason the phrase *functional symbolic trajectory* is useful. It describes not only the content of the present work, but also the task of presenting it.

Reading and writing as shared trajectory work

If words are functional symbolic trajectories, then reading changes. Reading is not the extraction of fixed meaning from containers. Reading is reconstruction. The

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reader follows marks and rebuilds a path using context, memory, training, expectation, and correction.

Writing changes as well. Writing is not the insertion of perfect meanings into words. Writing is the laying down of a path that another mind may be able to follow.

This explains why exposition is difficult, especially for new work. A new phrase cannot be understood merely by being defined once. It must be used, varied, returned to, tested, contrasted, and repaired. The reader must learn the path.

It also explains why compression is dangerous and necessary. Without compression, nothing can be carried. With too much compression, the path collapses. With the wrong compression, the reader is pulled into another basin of use. Good writing chooses compressions that preserve the needed path while removing enough detail for the reader to move.

This is also why summaries are imperfect. A summary is a compression of a trajectory. It may preserve the main path, or it may preserve the wrong shape. In ordinary work, this is manageable. In frontier work, where the path itself is still forming, summary can be especially risky. It may compress away the very uncertainty that mattered.

The functional symbolic trajectory therefore gives a practical guide for writing:

Introduce the path gently.

Avoid inherited words that pull too strongly in the wrong direction.

Declare new terms plainly.

Repeat them in varied contexts.

Show examples.

Show failures.

Show return to measurement or use.

Allow uncertainty to remain visible.

This is not a decorative writing method. It is part of the work.

Functional symbolic trajectories and Geofinitism/FSM

Within Geofinitism/FSM, symbols are not treated as perfect copies of a directly held external world. A measurement passes through a boundary of finite distinction and becomes symbolic. The symbol is what can be held, compared, repeated, written, calculated, or shared. This does not make the symbol arbitrary. It makes it finite.

The functional symbolic trajectory fits naturally into this direction. It describes what happens after distinction has occurred. A symbol enters the endogenous symbolic

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space and begins to function. It can join other symbols. It can form equations, stories, theories, models, claims, and calculations. It can stabilise or drift. It can return to measurement or fail to do so.

The Alphonic Limit may later be used to mark the minimum symbolic distinction available within a given framework. In the present essay, the formal parameter α has been used more generally to denote symbolic resolution. This allows the idea to be introduced without requiring the full machinery of Geofinitism at the start.

The important point is that all symbolic work occurs under finite resolution. No word carries infinite detail. No equation carries every condition of its use. No model contains all possible measurements. No theory is the whole of what it describes. Everything that can be written, read, calculated, or transmitted is finite in its symbolic form.

This does not weaken symbolic work. It gives it a clearer base.

A functional symbolic trajectory is finite, but it may still be powerful. It is uncertain, but it may still be useful. It is compressed, but it may still carry structure. It is not perfect, but it may still guide action, prediction, measurement, and thought.

Limits of the phrase

The phrase *functional symbolic trajectory* should not be asked to do too much too quickly.

It does not mean that words are vague in a useless way.

It does not mean that all interpretations are equal.

It does not mean that mathematics is merely opinion.

It does not mean that science is only language.

It does not replace grammar, logic, measurement, engineering, or experiment.

It is a working description of how finite symbols behave in use.

Some trajectories are tightly constrained. Others are loose. Some are stable across centuries. Others collapse in a single conversation. Some return strongly to measurement. Others remain literary, emotional, speculative, or exploratory. Some symbols are repaired repeatedly. Others become so misleading that they need to be replaced.

The phrase is useful because it helps us ask better questions.

What is the symbol doing?

What path does it open?

What has it compressed?

What does it preserve?

What does it discard?

Where does uncertainty enter?

What constrains the movement?

Can the trajectory return to measurement, calculation, construction, or shared use?

These questions are practical. They help with reading, writing, theory-building, AI interpretation, mathematical exposition, and scientific method.

Conclusion: from fixed words to working paths

A word appears simple. It seems to stand still. But when examined in use, it moves.

It carries history. It compresses prior work. It unfolds through context. It is constrained by grammar, training, measurement, memory, and shared repair. It may narrow into formal calculation or widen into ordinary conversation. It may stabilise a field or misdirect one. It may survive for centuries or fail immediately.

The phrase *functional symbolic trajectory* gives a way to hold this movement without collapsing it into older terms

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that may carry unwanted paths. It treats a word as finite, symbolic, compressed, functional, and directional. It allows us to connect early marks and counting, geometrical construction, mathematical notation, Russell's useful fictions, Shannon's information theory, JPEG and modern compression, nonlinear dynamics, language models, and Geofinitism/FSM.

The central lesson is simple:

A word is not a thing we possess. A word is a path we learn to walk.

Some paths are ancient. Some are technical. Some are fragile. Some are newly made. Some are so well worn that we mistake them for the ground itself.

The work of careful thought is not to abandon symbols because they are imperfect. It is to understand how they move, how they compress, how they function, and how they may be repaired.

A functional symbolic trajectory is therefore not only a description of words. It is a method of care.

It asks us to notice the path before we trust the noun.

It asks us to preserve uncertainty without surrendering usefulness.

It asks us to build symbols that can be followed, tested, revised, and shared.

And in that sense, the phrase is itself a functional symbolic trajectory: a small compression of a larger journey, offered so that the next part of the path can be walked.

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